



COURSE DESCRIPTION CARD- SYLLABUS

Course name

Elements of general topology

Course

Field of study

Mathematics in Technology

Area of study (specialization)

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Level of study

first-cycle studies

Form of study

full-time

Year/Semester

3/5

Profile of study

general academic

Course offered in

Polish

Requirements

elective

Number of hours

Lectures

30

Tutorials

15

Laboratory classes

—

Projects/seminars

—

Other (e.g. online)

—

Number of credit points

4

Lecturers

Responsible for the course/lecturer::

prof. dr hab. Ryszard Płuciennik

Responsible for the course/lecturer::

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Prerequisites

Basic knowledge in domain of calculus, mathematical logic and set theory on the level of studies of the first-cycle. Ability to use the predicate calculus and quantifiers, language of the set theory, notions of convergence of sequences.

Course objective

In-depth knowledge of topology from scratch. Gaining the ability to apply the acquired knowledge to theoretical as well as practical issues in other fields of mathematics and physics.



Course-related learning outcomes

Knowledge

Knowledge of the most important theorems of general topology and their proofs. Understanding how to use the topology to other fields of mathematics with particular emphasis on mathematical analysis.

Skills

Ability to use notions of topological spaces, open sets, operation of closure, metric spaces, category method, separation axioms, metrizable of topological spaces. Ability to use these concepts for proving of various properties of topological spaces. Explanation of the meaning of geometric interpretation of these notions and using other tools of topology.

Social competences

Ability to precise formulation of mathematical problems and trying of solving them. Ability to search for information single-handedly in literature, also in English.

Methods for verifying learning outcomes and assessment criteria

Learning outcomes presented above are verified as follows:

Lectures: valuation of knowledge and skills during written test.

Tutorials: two large tests concerning an application of knowledge from the lectures in exercises (student can use his own notes). Systematic control of theoretical knowledge in form of short quizzes. Valuation of student answers during lessons. Valuation of activity during lessons.

Programme content

Update: 31.01.2020r.

Metric spaces and examples of them. The notion of topology. Methods of Topological constructions. the quotient topology. Induced topologies. Separation axioms and relationships between them. Continuity of functions in topological spaces. Conditions equivalent to continuity. The notion of compact set and connected set. Properties of compact sets. Properties of real functions defined on compact sets. Complete metric spaces. Banach fixed point theorem and its application to numerical solving of differential and integral equations. Cantor theorem. Baire theorem and its applications. Baire category methods.

Teaching methods

Lectures:

- the lecture conducted in an interactive way with formulating questions for a group of students or for selected students;
- the theory presented in relation to the current knowledge of students;
- student activity during classes is taken into account when the final grade is considered;

Tutorials:

- solving sample tasks on the board;
- detailed reviewing of task solutions and discussions with comments;



- initiating discussions on solutions.

Bibliography

Basic

- R. Engelking, Topologia ogólna, Wydawnictwo Naukowe PWN Warszawa 2012.
- K. Jänich, Topologia, PWN Warszawa 1996.

Additional

- K. Kuratowski, Wstęp do teorii mnogości i topologii, Wydawnictwo Naukowe PWN Warszawa 2004.

Breakdown of average student's workload

	Hours	ECTS
Total workload	120	4,0
Classes requiring direct contact with the teacher	60	2,0
Student's own work (literature studies, preparation for laboratory classes/tutorials, preparation for tests/exam, project preparation)	60	2,0